

## Visualisation and interpretation of uncertainty and variability in Industrial Ecology

Leonardo Paoli

**Resource Efficiency Collective** 



- 1. What can we learn from uncertainty and variability analysis?
- 2. Uncertainty and variability analysis insights
- 3. Examples of uncertainty and variability visualisation
- 4. Summary and Discussion Prompt



## What can we learn from uncertainty and variability analysis?



![](_page_2_Picture_2.jpeg)

![](_page_3_Figure_1.jpeg)

 $A = X_1 \pm \alpha$ 

![](_page_3_Picture_3.jpeg)

![](_page_4_Figure_1.jpeg)

![](_page_4_Figure_2.jpeg)

 $A = X_1 \pm \alpha \qquad B = X_2 \pm \beta$ 

 $\beta > \alpha$  therefore B more uncertain than A

![](_page_4_Picture_5.jpeg)

![](_page_5_Figure_1.jpeg)

 $A = X_1 \pm \alpha$   $B = X_2 \pm \beta$ 

X% probability that B>A

![](_page_5_Picture_4.jpeg)

![](_page_6_Figure_1.jpeg)

#### **Uncertainty source**

 Combination of magnitude and centrality of uncertain flow

![](_page_6_Picture_4.jpeg)

![](_page_7_Figure_1.jpeg)

#### **Probability of reaching**

- Critical values
- Benchmarks

![](_page_7_Picture_5.jpeg)

### Visualising Uncertainty and Variability in Industrial Ecology

![](_page_8_Picture_1.jpeg)

#### Example1 – Sankey – Material Flow Analysis

![](_page_9_Figure_1.jpeg)

Laner, David, Helmut Rechberger, and Thomas Astrup. "Applying fuzzy and probabilistic uncertainty concepts to the material flow analysis of palladium in Austria." *Journal of Industrial Ecology* 19.6 (2015): 1055-1069.

![](_page_9_Picture_3.jpeg)

### **Example 2 – Sankey – Energy Flow Analysis**

![](_page_10_Figure_1.jpeg)

Paoli Leonardo, Lupton Richard, and Cullen Jonathan. "Probabilistic model allocating primary energy to end-use devices." *Energy Procedia* - accepted

![](_page_10_Picture_3.jpeg)

#### **Example 3 – Violin Plot – Energy Flow Analysis**

![](_page_11_Figure_1.jpeg)

Paoli Leonardo, Lupton Richard, and Jonathan Cullen. "Probabilistic model allocating primary energy to end-use devices." *Energy Procedia* - accepted

![](_page_11_Picture_3.jpeg)

#### **Example 4 – Line Plot – Input Output**

![](_page_12_Figure_1.jpeg)

Lenzen, Manfred, Richard Wood, and Thomas Wiedmann. "Uncertainty analysis for multi-region input–output models–a case study of the UK's carbon footprint." *Economic Systems Research* 22.1 (2010): 43-63.

![](_page_12_Picture_3.jpeg)

#### **Example 5 – Line Plot – Variability**

![](_page_13_Figure_1.jpeg)

Light-Duty Automotive Technology, Carbon Dioxide Emissions, and Fuel Economy Trends: 1975 Through 2016, Environmental Protection Agency

![](_page_13_Picture_3.jpeg)

# Example 6 – Box and Whisker – Life Cycle Assessment

![](_page_14_Figure_1.jpeg)

![](_page_14_Figure_2.jpeg)

Sills, Deborah L., et al. "Quantitative uncertainty analysis of life cycle assessment for algal biofuel production." *Environmental science & technology* 47.2 (2012): 687-694.

![](_page_14_Picture_4.jpeg)

#### **Example 7 – Line Plot – Transport Modelling**

![](_page_15_Figure_1.jpeg)

Yan, Xiaoyu, and Adam M. Boies. "Quantifying the uncertainties in life cycle greenhouse gas emissions for UK wheat ethanol." *Environmental Research Letters* 8.1 (2013): 015024.

![](_page_15_Picture_3.jpeg)

#### **Summary of examples – Discussion prompt**

	MFA	LCA	I/O
Extreme case		Box-Whisker	
Uncertainty of comparison	Violin	Box-Whisker	Line Plot
Identification of knowledge gap	Sankey		
Comparison of uncertain results	Sankey, Violin	Box-Whisker	Line Plot
Uncertainty of result	Sankey, Violin		Line Plot
Variability			

![](_page_16_Picture_2.jpeg)

![](_page_17_Picture_0.jpeg)

![](_page_17_Picture_1.jpeg)